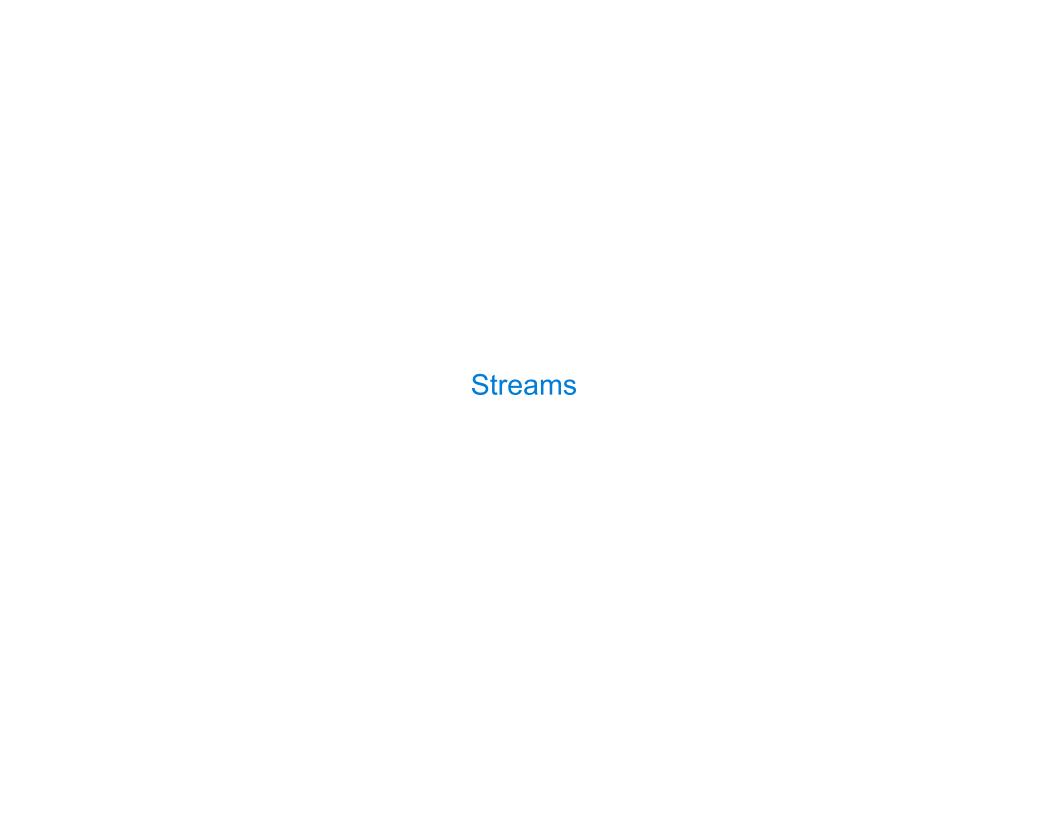


Efficient Sequence Processing

Sequence Operations

```
Map, filter, and reduce express sequence manipulation using compact expressions
Example: Sum all primes in an interval from a (inclusive) to b (exclusive)
          def sum_primes(a, b):
                                             def sum_primes(a, b):
              total = 0
                                                  return sum(filter(is prime, range(a, b)))
              x = a
                                             sum primes(1, 6)
              while x < b:
                  if is prime(x):
                                                                filter
                                                                               range iterator
                                                  sum
                      total = total + x
                                                   source: —
                  X = X + 1
                                                                 source: -
                                                                                next: 3
              return total
                                                    total: 200
                                                                                 end: 6
                                                                 f: is_prime
                   Constant
Space:
                                                           Also Constant
                                           (Demo)
```

-



Streams are Lazy Scheme Lists

```
A stream is a list, but the rest of the list is computed only when needed:
                                             (car (cons-stream 1 nil)) -> 1
 (car (cons 1 nil)) -> 1
 (cdr (cons 1 nil)) -> ()
                                             (cdr-stream (cons-stream 1 nil)) -> ()
 (cons 1 (cons 2 nil))
                                             (cons-stream 1 (cons-stream 2 nil))
Errors only occur when expressions are evaluated:
             1 (cons (/ 1 0) nil))
 (cons
                                                    -> ERROR
 (cons-stream 1 (cons-stream (/ 1 0) nil)) -> (1 . #[promise (not forced)])
            (cons-stream 1 (cons-stream (/ 1 0) nil))) -> 1
 (car
 (cdr-stream (cons-stream 1 (cons-stream (/ 1 0) nil))) -> ERROR
                                         (Demo)
```

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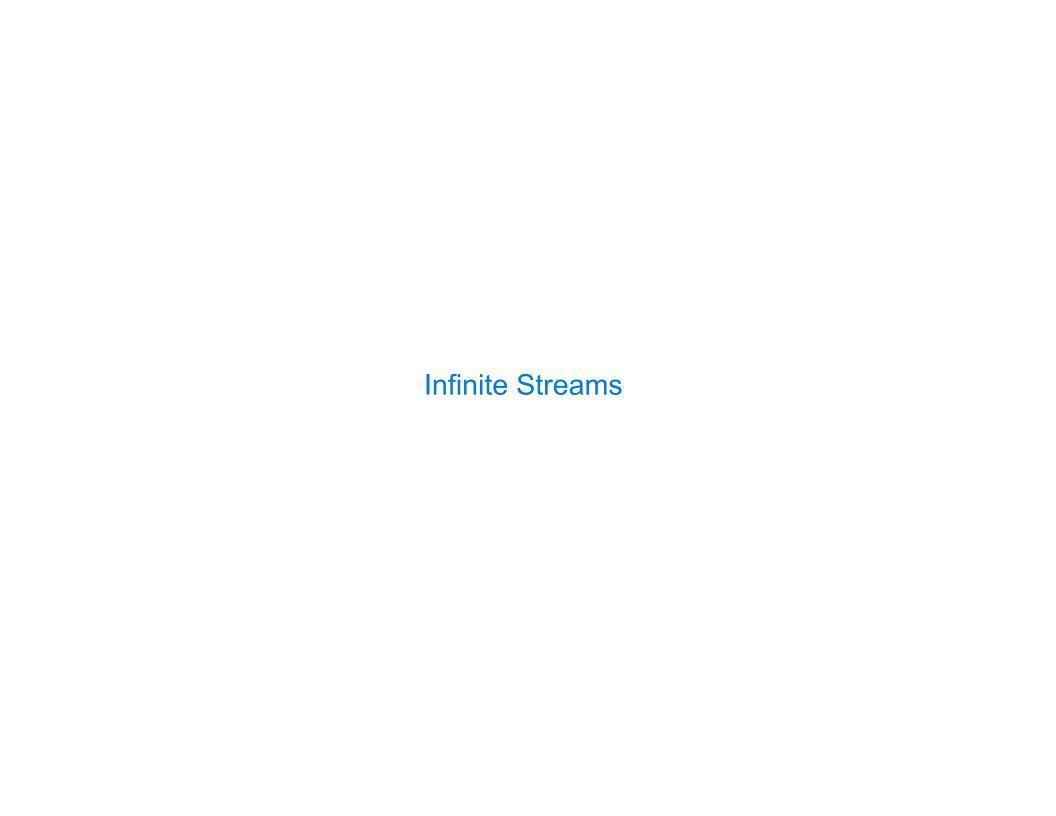
Stream Ranges are Implicit

```
A stream can give on-demand access to each element in order

(define (range-stream a b)
   (if (>= a b)
        nil
        (cons-stream a (range-stream (+ a 1) b))))

(define lots (range-stream 1 100000000000000000)))

scm> (car lots)
1
scm> (car (cdr-stream lots))
2
scm> (car (cdr-stream (cdr-stream lots)))
3
```



Integer Stream

```
An integer stream is a stream of consecutive integers

The rest of the stream is not yet computed when the stream is created

(define (int-stream start)
        (cons-stream start (int-stream (+ start 1))))
```

(Demo)

Stream Processing

(Demo)

Recursively Defined Streams

The rest of a constant stream is the constant stream

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Example: Repeats

```
(define a (cons-stream 1 (cons-stream 2 (cons-stream 3 a))))
(define (f s) (cons-stream (car s)
                           (cons-stream (car s)
                                         (f (cdr-stream s)))))
(define (g s) (cons-stream (car s)
                           (f (g (cdr-stream s)))))
What's (prefix (f a) 8)? ( \frac{1}{2} \frac{1}{2} \frac{2}{2} \frac{3}{3} \frac{3}{1} \frac{1}{1} )
What's (prefix (g a) 8)? (\frac{1}{2} \frac{2}{2} \frac{3}{3} \frac{3}{3} \frac{3}{4} )
```

Higher-Order Stream Functions

Higher-Order Functions on Streams

Implementations are identical, but change cons to cons-stream and change cdr to cdr-stream

```
(define (map-$ts\u00e0am f s)
  (if (null? s)
      nil
      (cons-$fréemr(f)(car s))
            (map-stream f
                 (cdr-stneam s)))))
(define (filter-$ts@am f s)
  (if (null? s)
      nil
      (if (f (car s))
          (cons-$taeam)(car s)
                (filter-$t(edm $)(odr-stream s)))
          (filter-$tream $)≬òdr-stream s)))))
(define (reduce-$treamaft) start)
  (if (null? s)
      start
      (reduce-ftream f
              (cdr-stream s)
              (f start (car s))))
```

A Stream of Primes

For any prime k, any larger prime must not be divisible by k.

The stream of integers not divisible by any k <= n is:

The stream of integers not divisible by any k < n

Filtered to remove any element divisible by n

This recurrence is called the Sieve of Eratosthenes

(Demo)