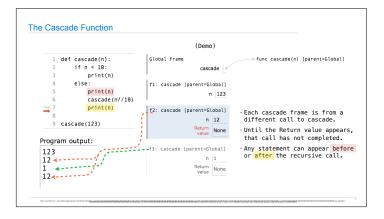


Order of Recursive Calls



```
Example: Inverse Cascade
```

```
Tree Recursion
```

Tree Recursion

Tree-shaped processes arise whenever executing the body of a recursive function makes more than one recursive call

```
n: 0, 1, 2, 3, 4, 5, 6, 7, 8, ..., 35
fib(n): 0, 1, 1, 2, 3, 5, 8, 13, 21, ..., 9,227,465
```

def fib(n):
 if n == 0:
 return 0
 elif n == 1:
 return 1
 else:
 return fib(n-2) + fib(n-1)

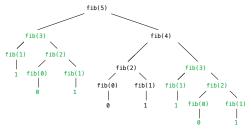


http://en.wikipedia.org/wiki/File:Fibonacci.jpg

A Tree-Recursive Process The computational process of fib evolves into a tree structure fib(4) fib(3) 🗨 fib(1) fib(2) fib(2) 💣 fib(3) fib(0) fib(1) fib(0) fib(1) fib(1) fib(0) fib(1) (Demo)

Repetition in Tree-Recursive Computation

This process is highly repetitive; fib is called on the same argument multiple times

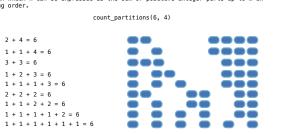


(We will speed up this computation dramatically in a few weeks by remembering results)

Example: Counting Partitions

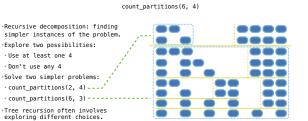
Counting Partitions

The number of partitions of a positive integer n, using parts up to size m, is the number of ways in which n can be expressed as the sum of positive integer parts up to m in increasing order.



Counting Partitions

The number of partitions of a positive integer n, using parts up to size m, is the number of ways in which n can be expressed as the sum of positive integer parts up to m in non-decreasing order.



Counting Partitions

The number of partitions of a positive integer n, using parts up to size m, is the number of ways in which n can be expressed as the sum of positive integer parts up to m in increasing order.

