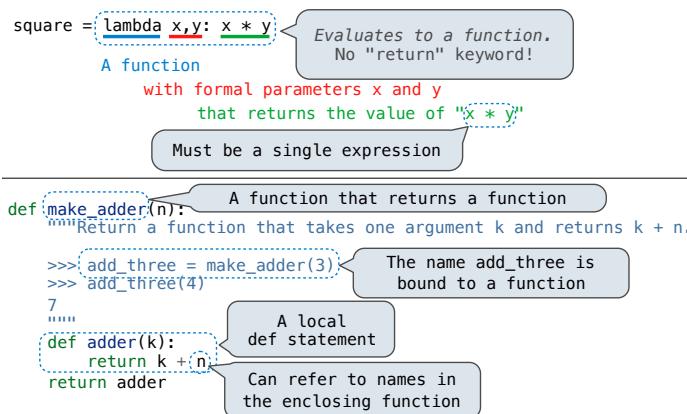


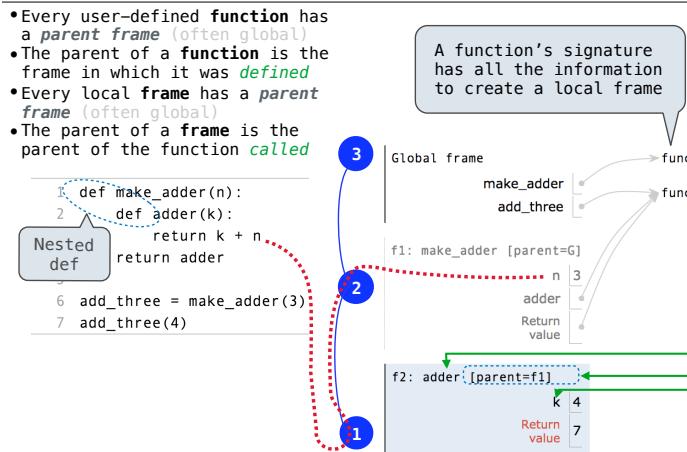
<p>Import statement:</p> <pre>1 from math import pi 2 tau = 2 * pi</pre> <p>Assignment statement:</p> <pre>1 tau = 2 * pi</pre> <p>Code (left): Statements and expressions Red arrow points to next line. Gray arrow points to the line just executed</p> <p>Frames (right): A name is bound to a value In a frame, there is at most one binding per name</p>	
<pre>1 from operator import mul 2 def square(x): 3 return mul(x, x) 4 square(-2)</pre> <p>Global frame: Intrinsic name of function called: <code>mul</code> Formal parameter bound to argument: <code>x</code> Return value: <code>4</code></p> <p>Built-in function: <code>func mul(...)</code> [parent=Global] <code>func square(x)</code> [parent=Global]</p> <p>User-defined function: <code>f1: square [parent=Global]</code></p> <p>Local frame: Return value is not a binding!</p>	
<pre>1 from operator import mul 2 def square(x): 3 return mul(x, x) 4 square(square(3))</pre> <p>A name evaluates to the value bound to that name in the earliest frame of the current environment in which that name is found.</p> <p>Global frame: <code>mul</code> <code>square</code> <code>f1: square [parent=Global]</code> <code>x 3</code> Return value: <code>9</code></p> <p>Local frame: <code>f2: square [parent=Global]</code> <code>x 9</code> Return value: <code>81</code></p>	
<p>Evaluation rule for call expressions:</p> <ol style="list-style-type: none"> Evaluate the operator and operand subexpressions. Apply the function that is the value of the operator subexpression to the arguments that are the values of the operand subexpressions. 	
<p>Applying user-defined functions:</p> <ol style="list-style-type: none"> Create a new local frame with the same parent as the function that was applied. Bind the arguments to the function's formal parameter names in that frame. Execute the body of the function in the environment beginning at that frame. 	
<p>Execution rule for def statements:</p> <ol style="list-style-type: none"> Create a new function value with the specified name, formal parameters, and function body. Its parent is the first frame of the current environment. Bind the name of the function to the function value in the first frame of the current environment. 	
<p>Execution rule for assignment statements:</p> <ol style="list-style-type: none"> Evaluate the expression(s) on the right of the equal sign. Simultaneously bind the names on the left to those values, in the first frame of the current environment. 	
<p>Execution rule for conditional statements:</p> <ol style="list-style-type: none"> Each clause is considered in order. Evaluate the header's expression. If it is a true value, execute the suite, then skip the remaining clauses in the statement. 	
<p>Evaluation rule for or expressions:</p> <ol style="list-style-type: none"> Evaluate the subexpression <left>. If the result is a true value v, then the expression evaluates to v. Otherwise, the expression evaluates to the value of the subexpression <right>. 	
<p>Evaluation rule for and expressions:</p> <ol style="list-style-type: none"> Evaluate the subexpression <left>. If the result is a false value v, then the expression evaluates to v. Otherwise, the expression evaluates to the value of the subexpression <right>. 	
<p>Evaluation rule for not expressions:</p> <ol style="list-style-type: none"> Evaluate <exp>; The value is True if the result is a false value, and False otherwise. 	
<p>Execution rule for while statements:</p> <ol style="list-style-type: none"> Evaluate the header's expression. If it is a true value, execute the (whole) suite, then return to step 1. 	
<p>Pure Functions:</p> <pre>-2 ► abs(number): 2</pre> <p>Non-Pure Functions:</p> <pre>2, 10 ► pow(x, y): 1024</pre> <p>Compound statement:</p> <pre><header>: <statement> <separating header>: <statement> ... <statement></pre> <p>def abs_value(x):</p> <pre>1 statement, 3 clauses, 3 headers, 3 suites, 2 boolean contexts</pre> <p>if x > 0: </p> <p>elif x == 0: </p> <p>else: </p>	<p>Higer-order function: A function that takes a function as an argument value or returns a function as a return value</p> <p>Nested def statements: Functions defined within other function bodies are bound to names in the local frame</p>



VS

```
def square(x):
    return x * x
```

- Both create a function with the same domain, range, and behavior.
- Both functions have as their parent the environment in which they were defined.
- Both bind that function to the name square.
- Only the def statement gives the function an intrinsic name.



When a function is defined:

- Create a **function value**: func <name>(<formal parameters>)
- Its parent is the current frame.

f1: make_adder func adder(k) [parent=f1]

- Bind <name> to the **function value** in the current frame (which is the first frame of the current environment).

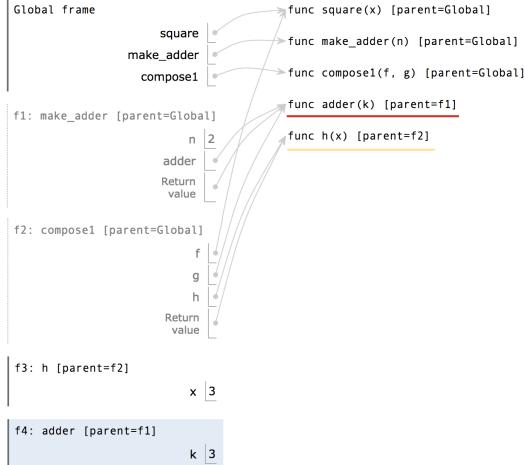
When a function is called:

- Add a **local frame**, titled with the <name> of the function being called.
- Copy the parent of the function to the **local frame**: [parent=<label>]
- Bind the <formal parameters> to the arguments in the **local frame**.
- Execute the body of the function in the environment that starts with the **local frame**.

```
>>> min(2, 1, 4, 3)  >>> 2 + 3
1                         5
>>> max(2, 1, 4, 3)  >>> 2 * 3
4                         6
>>> abs(-2)           >>> 2 ** 3
2                         8
>>> pow(2, 3)          >>> 5 / 3
8                         1.6666666666666667
>>> len('word')         >>> 5 // 3
4                         1
>>> round(1.75)        >>> 5 % 3
2                         2
>>> print(1, 2)
1 2
```

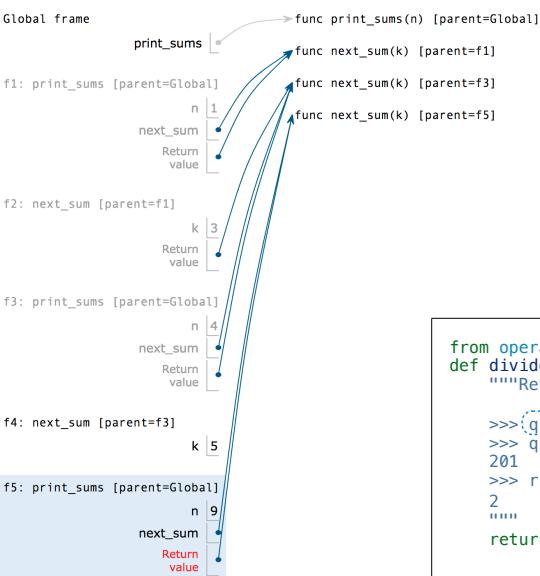
```
1 def square(x):
2     return x * x
3
4 def make_adder(n):
5     def adder(k):
6         return k + n
7     return adder
8
9 def compose1(f, g):
10    def h(x):
11        return f(g(x))
12    return h
13
14 compose1(square, make_adder(2))(3)
```

Return value of make_adder is an argument to compose1



```
1 def print_sums(n):
2     print(n)
3     def next_sum(k):
4         return print_sums(n+k)
5     return next_sum
6
7 print_sums(1)(3)(5)
```

Printed output:
1
4
9



```
def search(f):
    """Return the smallest non-negative integer x for which f(x) is a true value.
    """
    x = 0
    while True:
        if f(x):
            return x
        x += 1

def is_three(x):
    """Return whether x is three.

    >>> search(is_three)
    3
    """
    return x == 3

def inverse(f):
    """Return a function g(y) that returns x such that f(x) == y.

    >>> sqrt = inverse(lambda x: x * x)
    >>> sqrt(16)
    4
    """
    return lambda y: search(lambda x: f(x)==y)
```

False values so far: 0, False, '', None

Anything value that's not false is true.

```
>>> if 0:                  >>> if 1 and 0:
...     print('*')           ...     print('*')
>>> if 1:                  >>> if 1 or 0:
...     print('*')           ...     print('*')
*                                *
>>> if abs:                >>> if 1 or 1/0:
...     print('*')           ...     print('*')
*                                *
```

```
from operator import floordiv, mod
def divide_exact(n, d):
    """Return the quotient and remainder of dividing N by D.

    >>> q, r = divide_exact(2012, 10)
    201
    2
    """
    return floordiv(n, d), mod(n, d)
```

Multiple assignment to two names
Two return values, separated by commas